



Solid-state quantum memories for quantum repeaters

F. Bussières, C. Clausen, N. Timoney, I. Usmani, P. Jobez,
N. Sangouard, M. Afzelius, N. Gisin

11 September 2012



Quantum communication at a distance



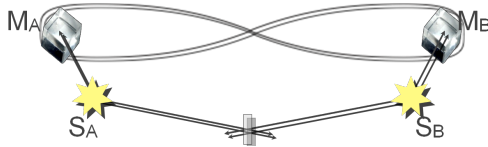
State of the art from **field** experiments

- Fibre length ~ 150 km * (250 km in the lab)
- Losses of 43 dB (0.29 dB/km)
- Base frequency > 300 MBits/s
- Secret bit key rate of 2.5 bits/s

Longer distances require new technologies : quantum repeaters and quantum networks

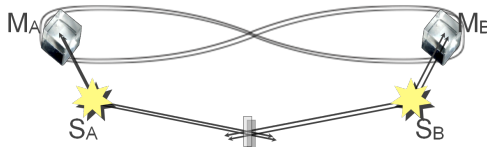
Quantum repeater

Creating entanglement

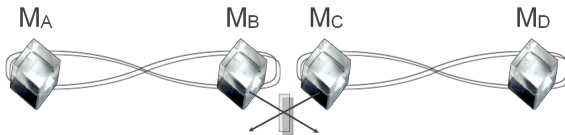


Quantum repeater

Creating entanglement

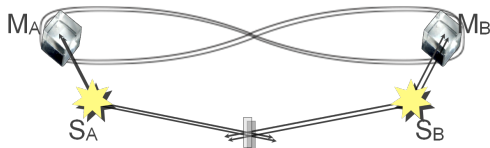


Entanglement swapping

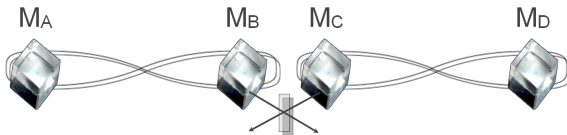


Quantum repeater

Creating entanglement



Entanglement swapping



Increasing the distance.





Quantum repeater: ingredients

- Efficient, long lived and multimode quantum memories
- Efficient quantum sources adapted to the memory bandwidth
- Efficient single photon detectors



Quantum memories in rare earth doped crystals

- Weak interaction with crystal environment.
 - “Atom” like energy structure on the 4f-4f transitions
 - “Frozen gas” of ions, no motional decoherence
- High number of stationary ions ($10^7 - 10^{10}$)
- Long optical coherence times ($T < 4\text{K}$), T_2^{opt} from μs -ms
- Long hyperfine coherence times ($T < 4\text{K}$), T_2^{hyp} from ms-s
- Large optical inhomogeneous broadening 100 MHz – 10 GHz
- Light storage times great than 1 s *



Quantum memories in rare earth doped crystals

- Weak interaction with crystal environment.
 - “Atom” like energy structure on the 4f-4f transitions
 - “Frozen gas” of ions, no motional decoherence
- High number of stationary ions ($10^7 - 10^{10}$)
- Long optical coherence times ($T < 4\text{K}$), T_2^{opt} from μs -ms
- Long hyperfine coherence times ($T < 4\text{K}$), T_2^{hyp} from ms-s
- Large optical inhomogeneous broadening 100 MHz – 10 GHz
- Light storage times great than 1 s *

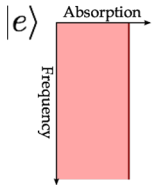
As quantum memories:

- 69 % storage efficiency**

* Longdell et al, PRL, 95, 06301 (2005), **Hedges et al, Nature 465, 1052 (2010)

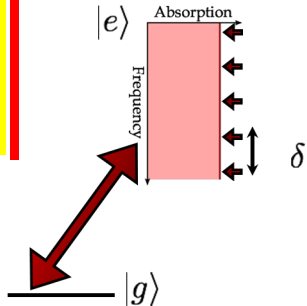


Quantum memory: AFC technique



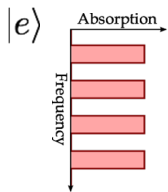


Quantum memory: AFC technique





Quantum memory: AFC technique



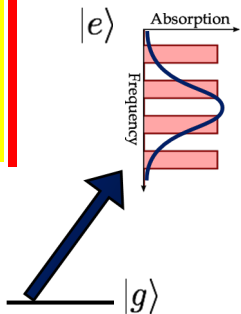
— $|g\rangle$



Quantum memory: AFC technique

State after absorption

$$\sum_{k=1}^N c_k |g_1 g_2 \dots e_k \dots g_N\rangle$$





Quantum memory: AFC technique

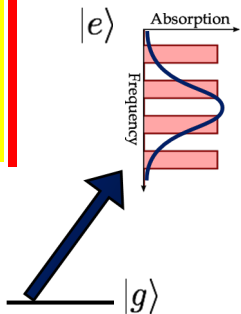
State after absorption

$$\sum_{k=1}^N c_k |g_1 g_2 \dots e_k \dots g_N\rangle$$

Dephasing occurs:

$$\sum_{k=1}^N c_k e^{-\delta_k t} |g_1 g_2 \dots e_k \dots g_N\rangle$$

$$\delta_k = m_k \Delta$$





Quantum memory: AFC technique

State after absorption

$$\sum_{k=1}^N c_k |g_1 g_2 \dots e_k \dots g_N\rangle$$

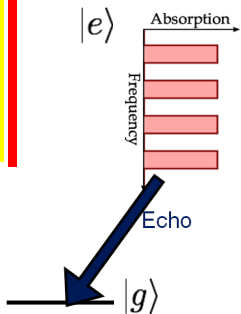
Dephasing occurs:

$$\sum_{k=1}^N c_k e^{-\delta_k t} |g_1 g_2 \dots e_k \dots g_N\rangle$$

$$\delta_k = m_k \Delta$$

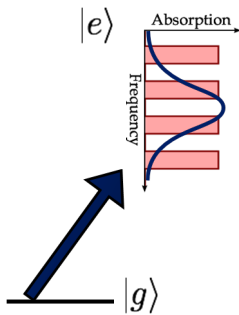
Rephasing after a time $t_e = \frac{2\pi}{\Delta}$

Collective emission in the forward mode. Photon echo like emission.



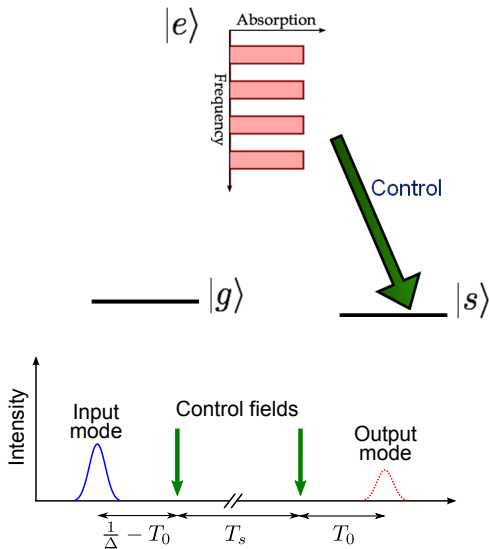


Full AFC scheme



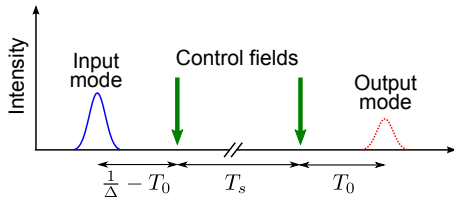
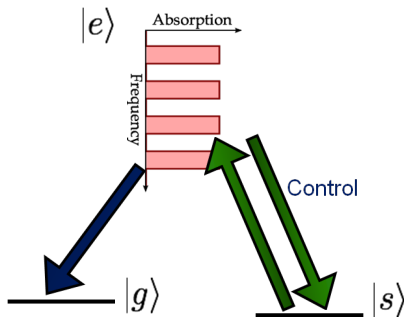


Full AFC scheme



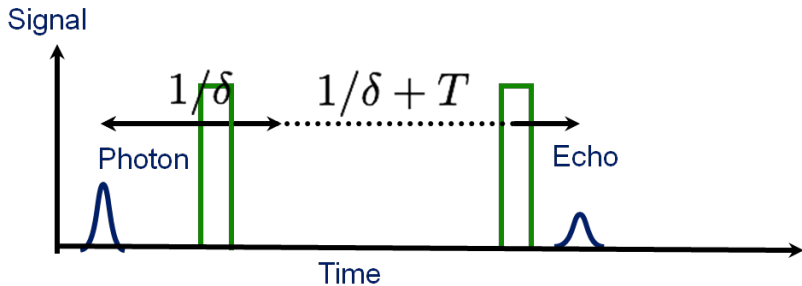


Full AFC scheme



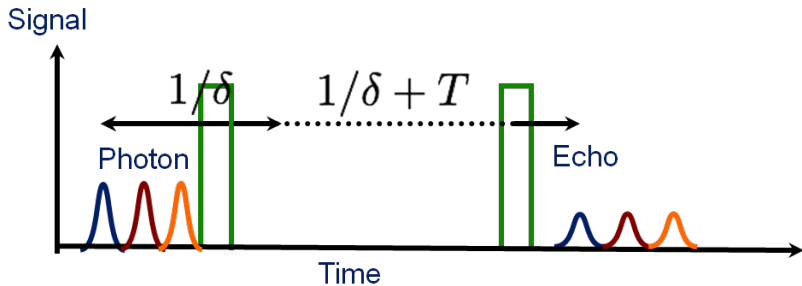


Multimode memory





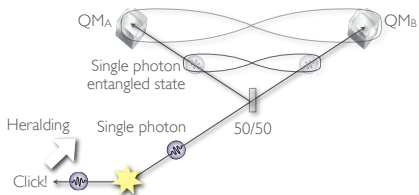
Multimode memory





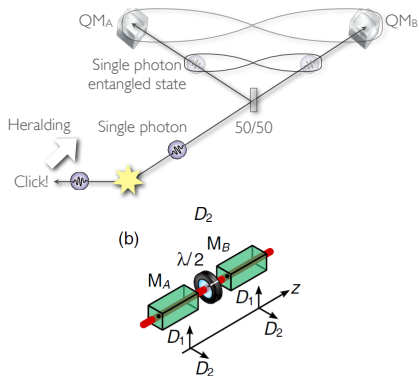
Outline

- Heralded entanglement of two crystals



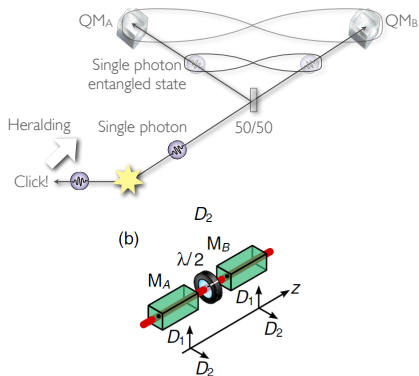
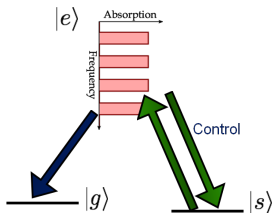
Outline

- Heralded entanglement of two crystals
- Storing polarization entanglement



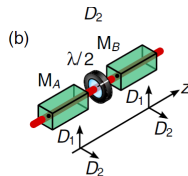
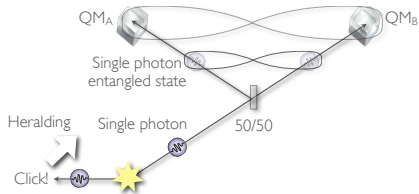
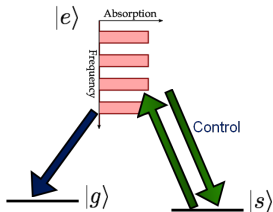
Outline

- Heralded entanglement of two crystals
- Storing polarization entanglement
- Long storage times in an on demand memory.

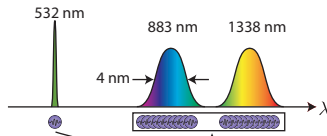
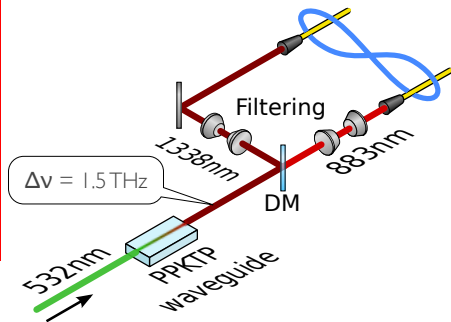


Outline

- **Heralded entanglement of two crystals**
- Storing polarization entanglement
- Long storage times in an on demand memory.

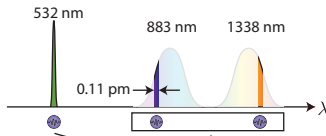
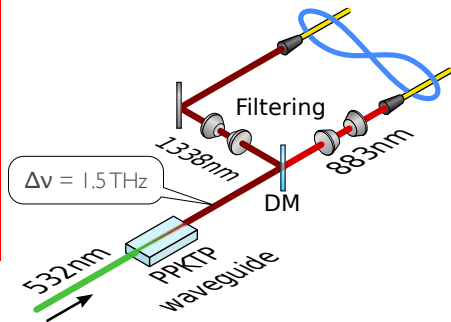


Photon pair source



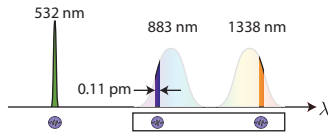
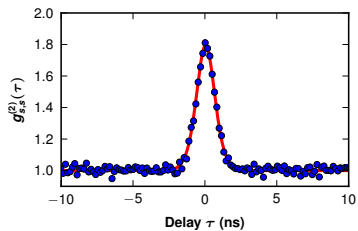
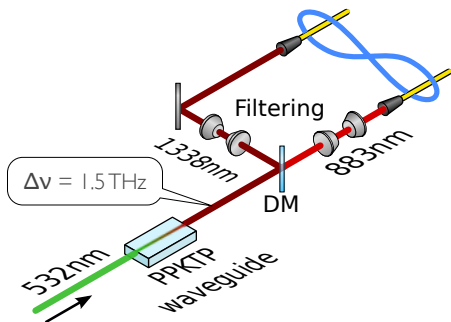


Photon pair source

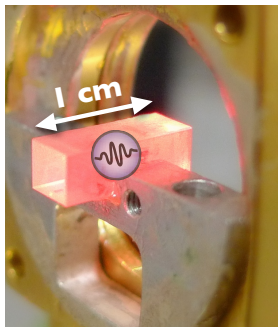




Photon pair source



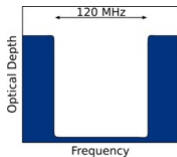
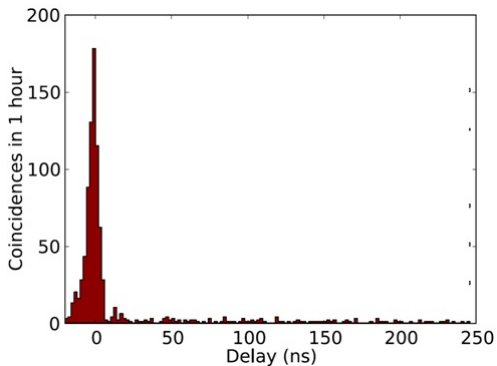
The memory



- Crystal : $\text{Nd}^{3+}:\text{Y}_2\text{SiO}_5$ (@ 3 K)
- $^4I_{9/2} \rightarrow ^4F_{3/2}$ (883 nm, $\Gamma_{inh} = 6$ GHz)
- $B_{ext} = 300$ mT (Zeeman split)
- AFC $1/\Delta$ from 30 ns to 1 μs



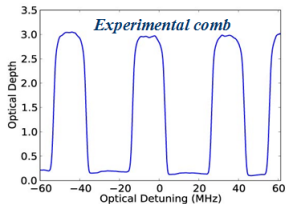
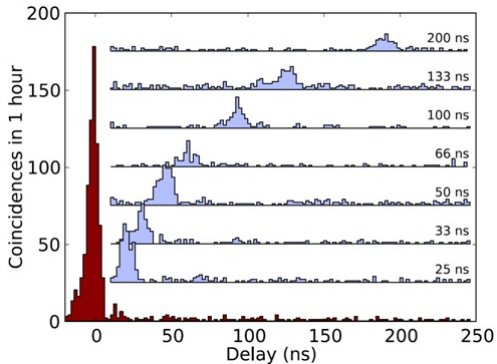
Heralding stored photon in the memory



Clausen et al, Nature, **469**,508 (2011)



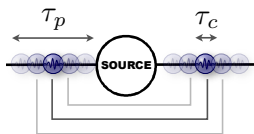
Heralding stored photon in the memory



Clausen et al, Nature, **469**,508 (2011)



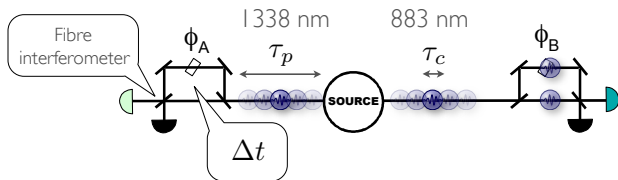
Storing photonic entanglement



Energy time entanglement

- Both photons are created simultaneously (τ_c)
- Creation time is uncertain (τ_p)

Storing photonic entanglement

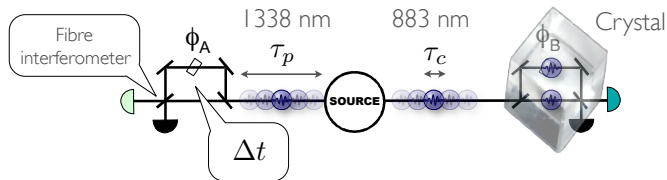


Energy time entanglement

- Both photons are created simultaneously (τ_c)
 - Creation time is uncertain (τ_p)
- Entanglement in the creation time (and thus their energies)

$$\tau_p \gg \Delta t \gg \tau_c$$

Storing photonic entanglement



Energy time entanglement

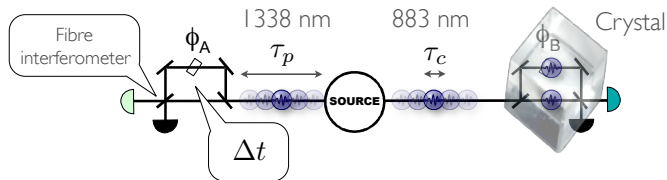
- Both photons are created simultaneously (τ_c)
 - Creation time is uncertain (τ_p)
- Entanglement in the creation time (and thus their energies)

Bell- CHSH inequality

- $S_{CHSH} \leq 2$ (Local bound)
- $S_Q = 2\sqrt{2}$ (Quantum bound)
- $S_{exp} = 2.64 \pm 0.23$

$$\tau_p \gg \Delta t \gg \tau_c$$

Storing photonic entanglement



Energy time entanglement

- Both photons are created simultaneously (τ_c)
 - Creation time is uncertain (τ_p)
- Entanglement in the creation time (and thus their energies)

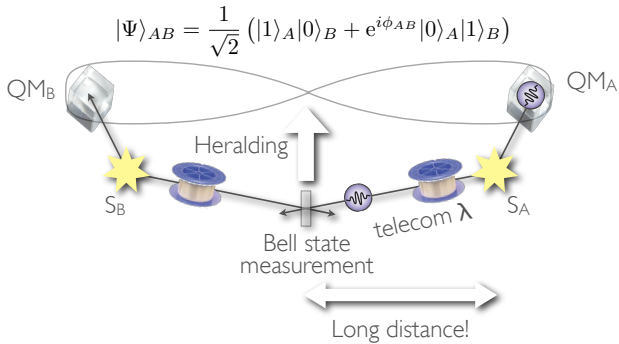
$$\tau_p \gg \Delta t \gg \tau_c$$

Bell- CHSH inequality

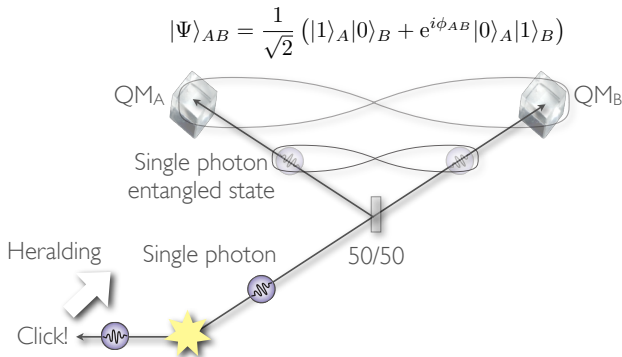
- $S_{CHSH} \leq 2$ (Local bound)
- $S_Q = 2\sqrt{2}$ (Quantum bound)
- $S_{exp} = 2.64 \pm 0.23$

Similar work in: Saglamyurek et al, Nature, **469**, 512 (2011)

Entangling two crystals



Entangling two crystals



- **Prior work** Nature **438**, 828 (2005), PRL **99**, 180504 (2007), Nature **452** 67 (2008), Polzik group (2001), Vuletic group (2007)
- **Related work** Science **334** 1253, (2011)



Entanglement?

- Ideal state : $\frac{1}{\sqrt{2}}(|1\rangle_A|0\rangle_B + |0\rangle_A|1\rangle_B)$
- Actual state:

$$\begin{pmatrix} p_{00} & 0 & 0 & 0 \\ 0 & p_{01} & d & 0 \\ 0 & d^* & p_{10} & 0 \\ 0 & 0 & 0 & p_{11} \end{pmatrix}$$

- $C \geq \max(0, V(p_{01} + p_{10})) - 2(p_{11} p_{00})^{\frac{1}{2}}$



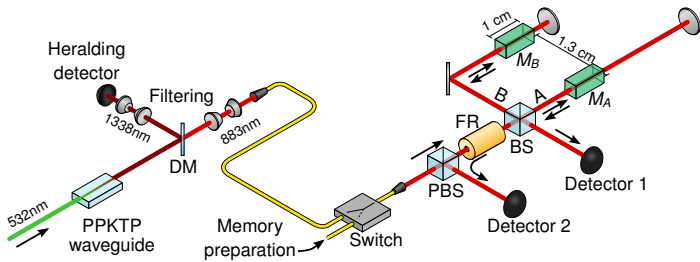
Entanglement?

- Ideal state : $\frac{1}{\sqrt{2}}(|1\rangle_A|0\rangle_B + |0\rangle_A|1\rangle_B)$
- Actual state:

$$\begin{pmatrix} p_{00} & 0 & 0 & 0 \\ 0 & p_{01} & d & 0 \\ 0 & d^* & p_{10} & 0 \\ 0 & 0 & 0 & p_{11} \end{pmatrix}$$

- $C \geq \max(0, V(p_{01} + p_{10})) - 2(p_{11} p_{00})^{\frac{1}{2}}$
- ✓ Single excitation terms
- ✓ Single excitation coherence
- × Loss
- × Two-photon term

Experiment to entangle two crystals



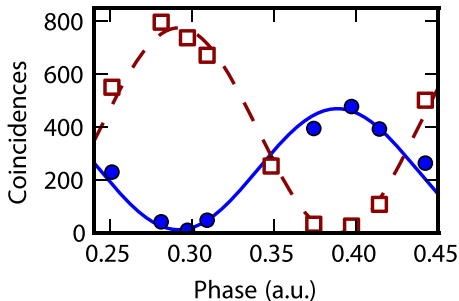
I Usmani et al, Nature Photonics, **6**, 234 (2012)



State tomography

$$C \geq \max(0, V(p_{01} + p_{10}) - 2\sqrt{p_{11}p_{00}})$$

- Lock and scan the interferometer to measure the visibility



- $V = 96.5 \pm 1.2\%$.
- Not enough to demonstrate entanglement.



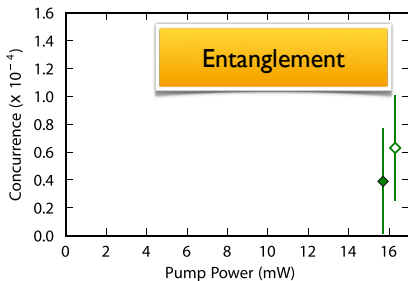
State tomography

$$C \geq \max(0, V(\rho_{01} + \rho_{10})) - 2(\rho_{11} \rho_{00})^{\frac{1}{2}}$$

- The interferometer was let drift over 166 hours, where 2 threefold coincidences were measured

Results:

- $\rho_{01} + \rho_{10} = 1.7777(34) \times 10^{-4}$
- $\rho_{00} = 0.999822$
- $\rho_{11} = (2.9 \pm 2.1) \times 10^{-9}$
- $V = 96.5 \pm 1.2\%$
- $C \geq (6.3 \pm 3.8) \times 10^{-5}$



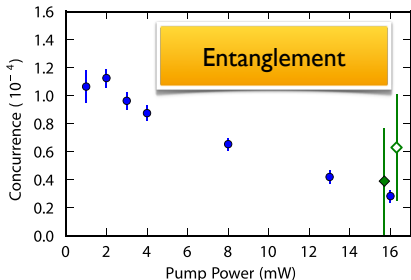


State tomography

Conservative assumption two-mode squeezed state $\rightarrow p_{11}$

Results:

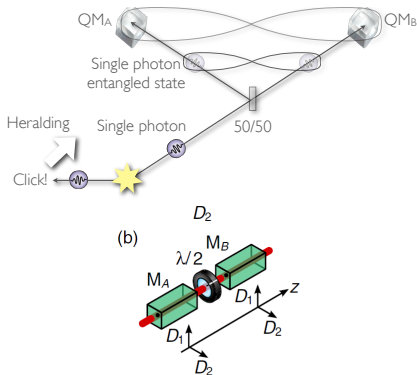
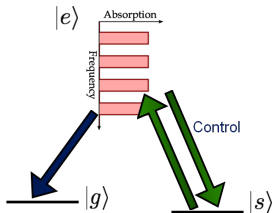
- $p_{01} + p_{10} = 1.7777(34) \times 10^{-4}$
- $p_{00} = 0.999822$
- $p_{11} = (2.9 \pm 2.1) \times 10^{-9}$
- $V = 96.5 \pm 1.2\%$



10^6 faster to get some statistics!

Outline

- Heralded entanglement of two crystals
- **Storing polarization entanglement**
- Long storage times in an on demand memory.

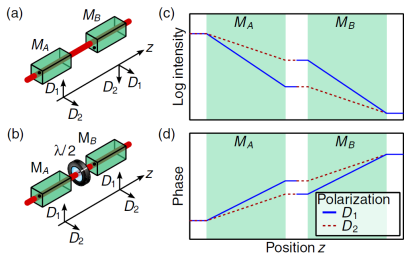




Storing polarization entanglement

- Crystals have two different indices of refraction in xy (d_1, d_2)
- Crystals have two absorption coefficients in xy (d_1, d_2)

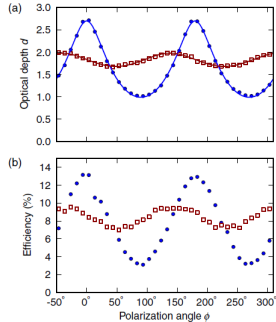
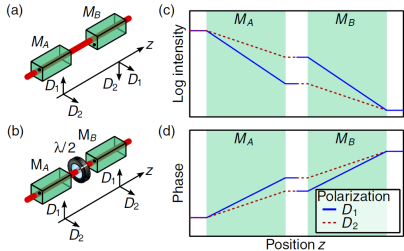
It is necessary to compensate for these effects



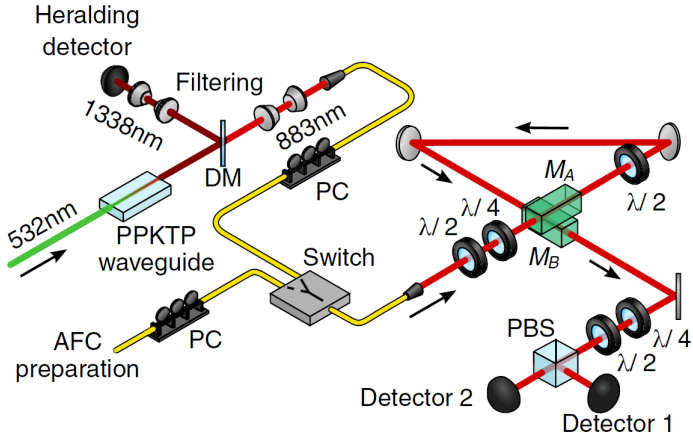
Storing polarization entanglement

- Crystals have two different indices of refraction in xy (d_1, d_2)
- Crystals have two absorption coefficients in xy (d_1, d_2)

It is necessary to compensate for these effects



Storing polarization entanglement



Auto correlation before storage $g_{s|i}^{(2)} < 0.06$



Storing polarization entanglement

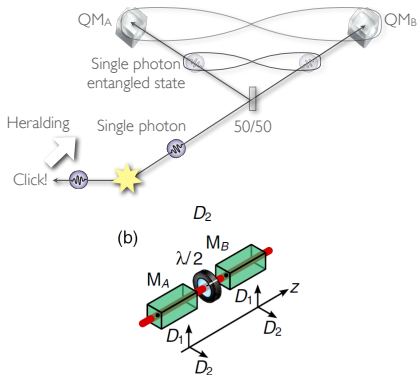
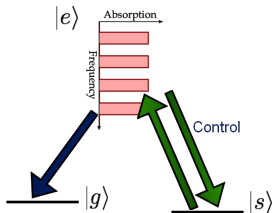
Input state	Fidelity	$\bar{g}_{si}^{(2)}$
$ H\rangle$	99.3(6)%	7.6(3)
$ V\rangle$	97(1)%	6.0(3)
$ L\rangle$	97.7(6)%	9.4(3)
$\frac{1}{\sqrt{2}}(H\rangle + V\rangle)$	95(1)%	8.0(3)
$\alpha H\rangle + \beta V\rangle$	98.7(9)%	9.2(3)

Similar work with weak coherent states in:

- Gündogan et al et al, PRL, **108**, 190504 (2012)
- Zhou et al, PRL, **108**, 190505 (2012)

Outline

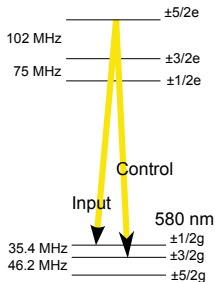
- Heralded entanglement of two crystals
- Storing polarization entanglement
- **Long storage times in an on demand memory.**





Candidate: Europium

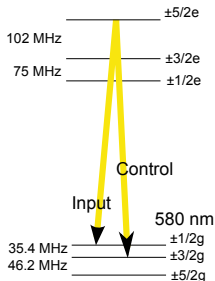
- Our sample (10 ppm) has an optical depth of 1.5 cm^{-1} and an inhomogeneous linewidth of 500 MHz
- The spin coherence time for $^{151}\text{Eu} \sim 15 \text{ ms}$ ($B = 0$)





Candidate: Europium

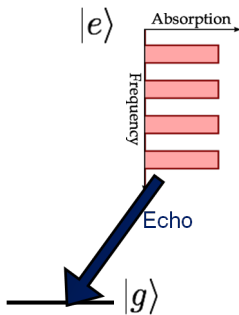
- Our sample (10 ppm) has an optical depth of 1.5 cm^{-1} and an inhomogeneous linewidth of 500 MHz
- The spin coherence time for $^{151}\text{Eu} \sim 15 \text{ ms}$ ($B = 0$)



- Optical depth of the input transition is 1 cm^{-1}
- Really good for a longlived multimode memory!

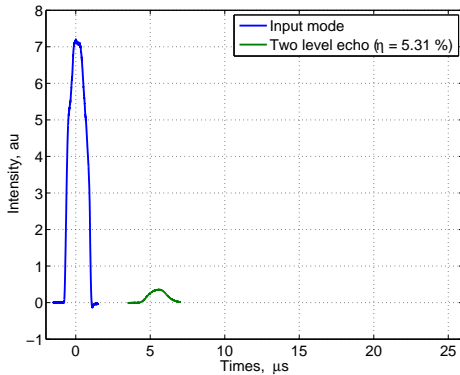


Two level echo



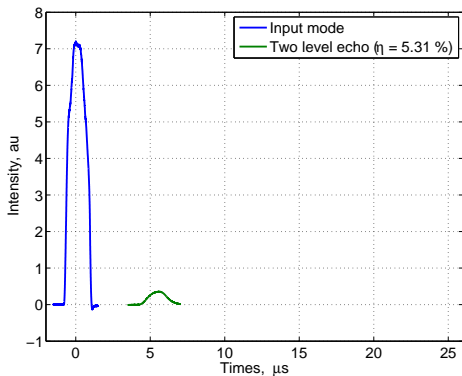


Two level echo efficiency





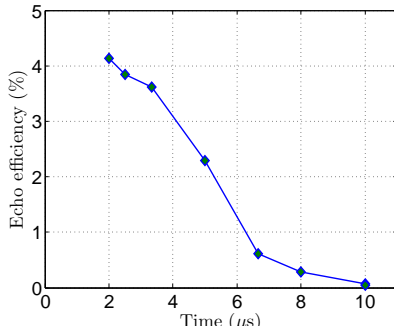
Two level echo efficiency



Comb spacing of 200 kHz \rightarrow 5 μs AFC

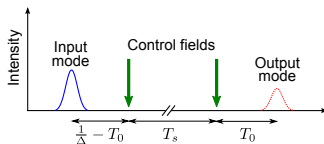
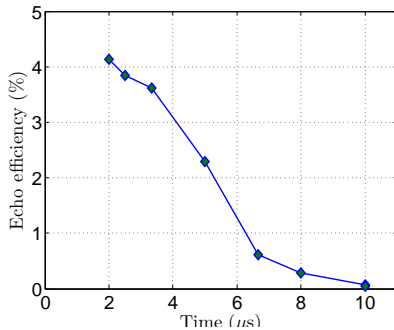


Laser linewidth limitation



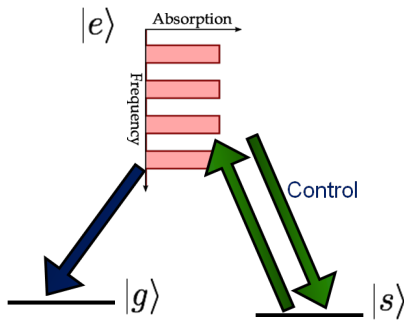


Laser linewidth limitation



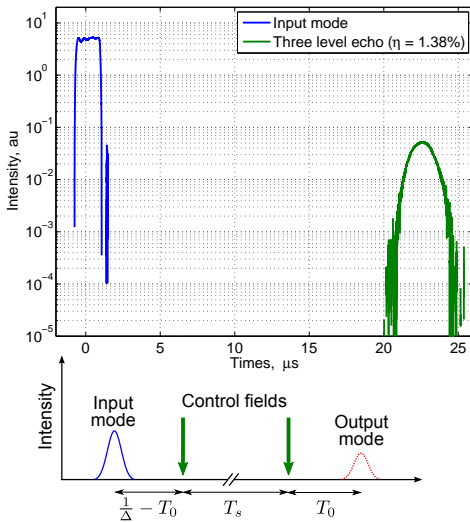


Spin wave storage

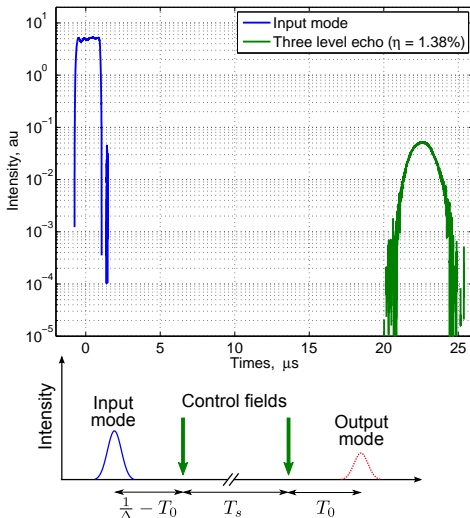




Spin wave storage

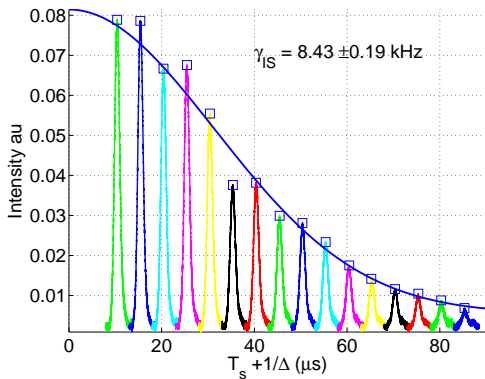


Spin wave storage



- Using square non chirped pulses estimate transfer efficiencies to be almost 50 %

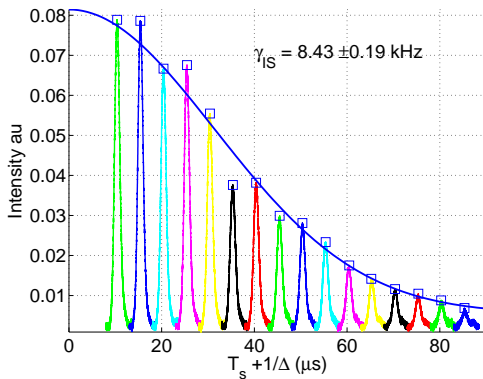
Inhomogeneous spin linewidth



$$\text{Echo height} = Ae^{\left(\frac{-t^2 \gamma_{IS}^2 \pi^2}{2 \ln 2}\right)}$$



Inhomogeneous spin linewidth

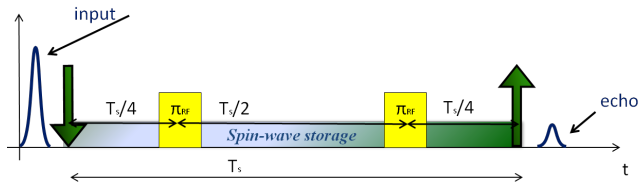


$$\text{Echo height} = Ae^{\left(\frac{-t^2 \gamma_{IS}^2 \pi^2}{2 \ln 2}\right)}$$

- Possible to use spin echo techniques to increase the lifetime *

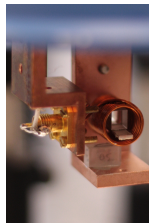
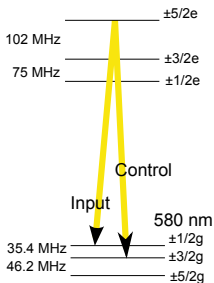
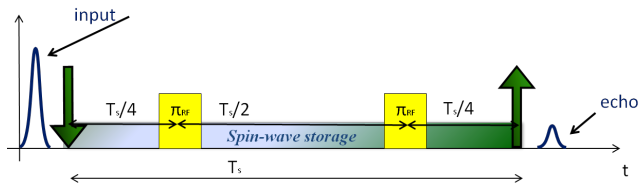


Overcoming inhomogeneous spin linewidth



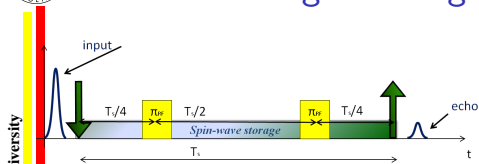


Overcoming inhomogeneous spin linewidth

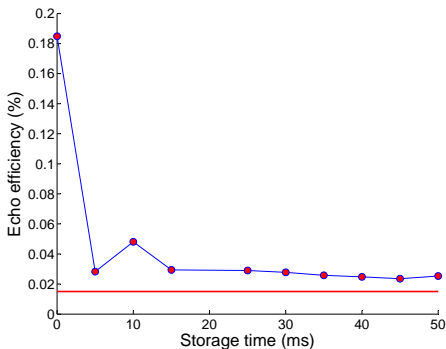




Overcoming inhomogeneous spin linewidth

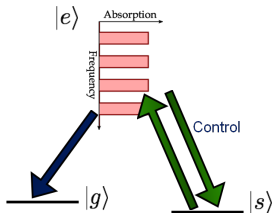


- Preliminary results
- Storage time of optical pulse for 50 ms!

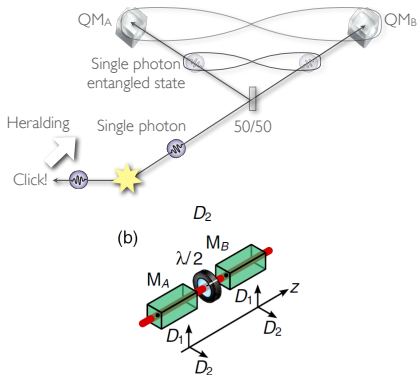


- Oscillation a quantum beat phenomenon?

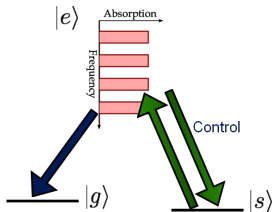
- Heralded entanglement of two crystals
- Storing polarization entanglement
- Long storage times in an on demand memory.



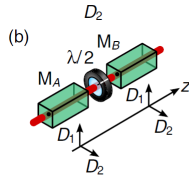
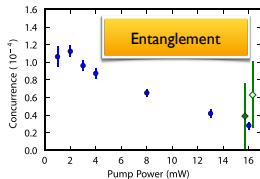
Summary



- **Heralded entanglement of two crystals**
- Storing polarization entanglement
- Long storage times in an on demand memory.

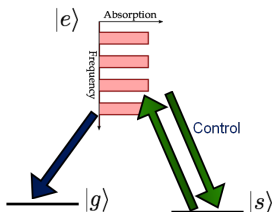


Summary

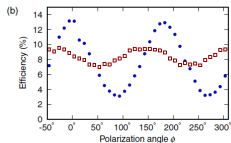
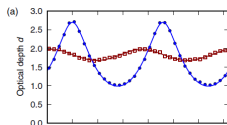
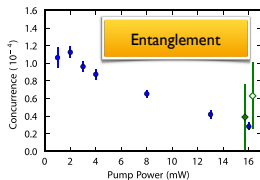




- Heralded entanglement of two crystals
- **Storing polarization entanglement**
- Long storage times in an on demand memory.

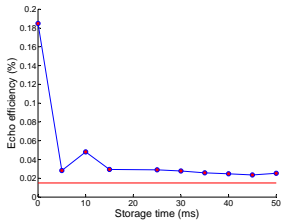


Summary

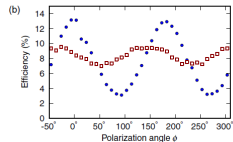
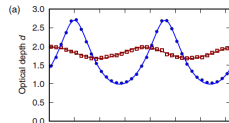
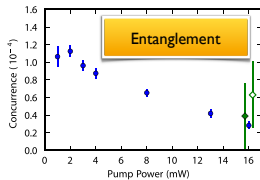




- Heralded entanglement of two crystals
- Storing polarization entanglement
- **Long storage times in an on demand memory.**



Summary





Outlook

- We will continue working with neodymium doped crystals as a test bench for storage and manipulation of quantum states of light



Outlook

- We will continue working with neodymium doped crystals as a test bench for storage and manipulation of quantum states of light
 - Current spectroscopic studies will reveal a suitable Λ -system for spin wave storage



Outlook

- We will continue working with neodymium doped crystals as a test bench for storage and manipulation of quantum states of light
 - Current spectroscopic studies will reveal a suitable Λ -system for spin wave storage
- In europium we are trying to obtain the result at the single photon storage level, we are implementing an impedance matched cavity to increase the storage efficiency and investigating using dynamical decoupling sequences to push the storage time beyond 50 ms



Outlook

- We will continue working with neodymium doped crystals as a test bench for storage and manipulation of quantum states of light
 - Current spectroscopic studies will reveal a suitable Λ -system for spin wave storage
- In europium we are trying to obtain the result at the single photon storage level, we are implementing an impedance matched cavity to increase the storage efficiency and investigating using dynamical decoupling sequences to push the storage time beyond 50 ms
- Our long term goal is to make an elementary quantum repeater link as long a distance as we can!

Thank you



Marie Curie Initial Training Network
Coherent Information Processing
in Rare-Earth Ion Doped Solids



We are grateful to Y Sun, R L Cone and RM Macfarlane for kindly lending us the $^{151}\text{Eu}^{3+}$ doped Y_2SiO_5 crystal.